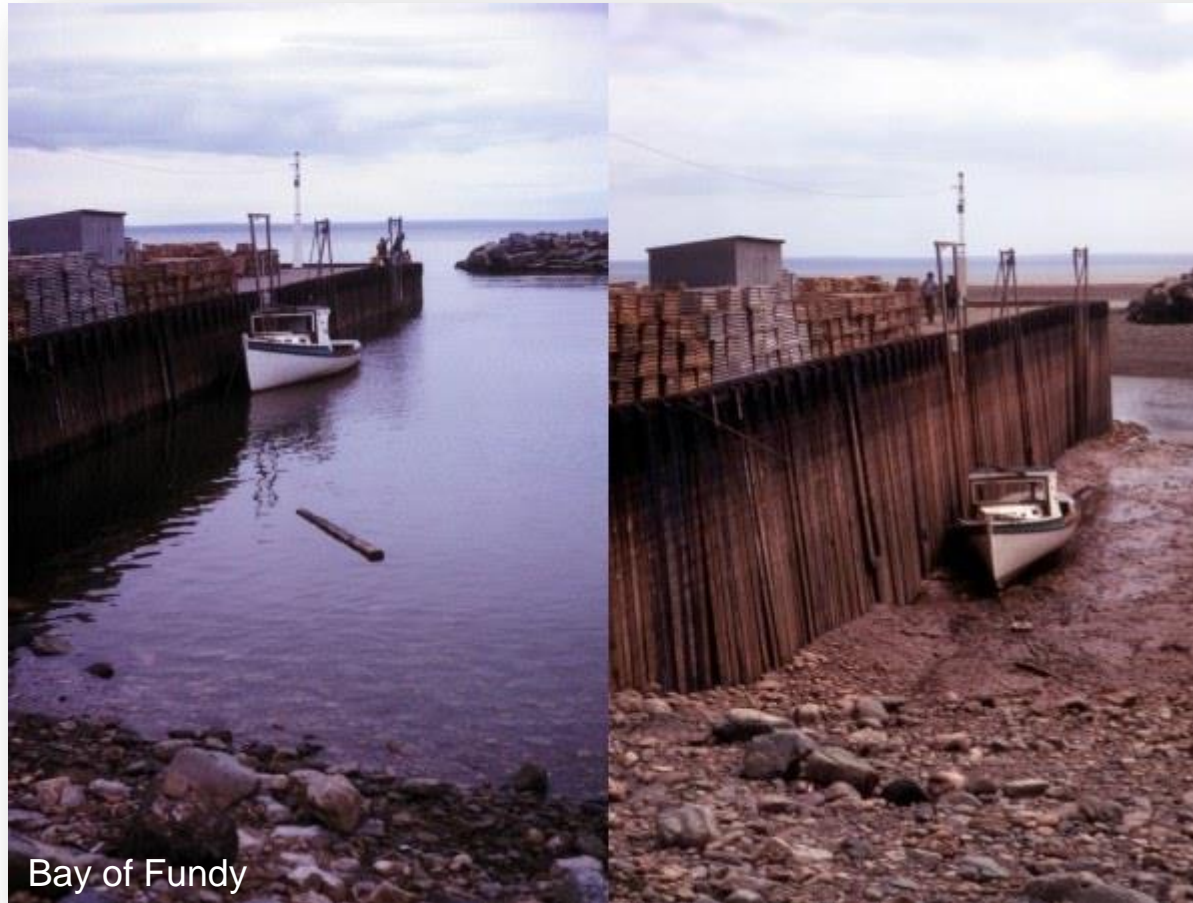


Optimizing Tides in Barotropic HYCOM



Objectives

- Improve tidal water levels and currents in HYCOM with the best available internal wave drag scheme
- Better surface tides give better internal tides in HYCOM
- Improved tidal prediction skills allows HYCOM to be used for nesting (internal) tides in regional models

Barotropic Tide Model

- One layer momentum equation

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} + f \hat{k} \times \mathbf{u} = -g \nabla (\eta - \eta_{EQ} - \eta_{SAL}) - \frac{C_d |\mathbf{u}| \mathbf{u}}{H} - \frac{C \mathbf{u}}{\rho_0 H} + \mathcal{F}$$

forcing
bottom drag
int. w. drag

- Global tripolar grid with $2/25^\circ$ resolution
- M_2 equilibrium tide and spatially varying scalar Self Attraction and Loading $\eta_{SAL} = \beta(x, y) \cdot \eta$
- First* find best RMS by varying linear internal wave drag, *then* iterate SAL
- Model is run for 33 days; last three days are analyzed

Internal Wave Drag Schemes

- Jayne and St Laurent (2001) scalar:

$$C_{JSL} = \frac{\pi}{L} \tilde{H}^2 N_b$$

- Nycander (2005) tensor:

$$\mathbb{C} = \frac{N_b}{4\pi} \sqrt{1 - \frac{f^2}{\omega^2}} (\nabla h \nabla J + \nabla J \nabla h) = \begin{bmatrix} C_{xx} & C_{xy} \\ C_{yx} & C_{yy} \end{bmatrix}$$

- Nycander scalar

$$C_{NC} = \frac{\langle D_{\mathbb{C}} \rangle}{\rho_0 \langle |\mathbf{u}|^2 \rangle} = \frac{\langle \mathbf{u} \cdot \mathbb{C} \cdot \mathbf{u} \rangle}{\langle |\mathbf{u}|^2 \rangle}$$

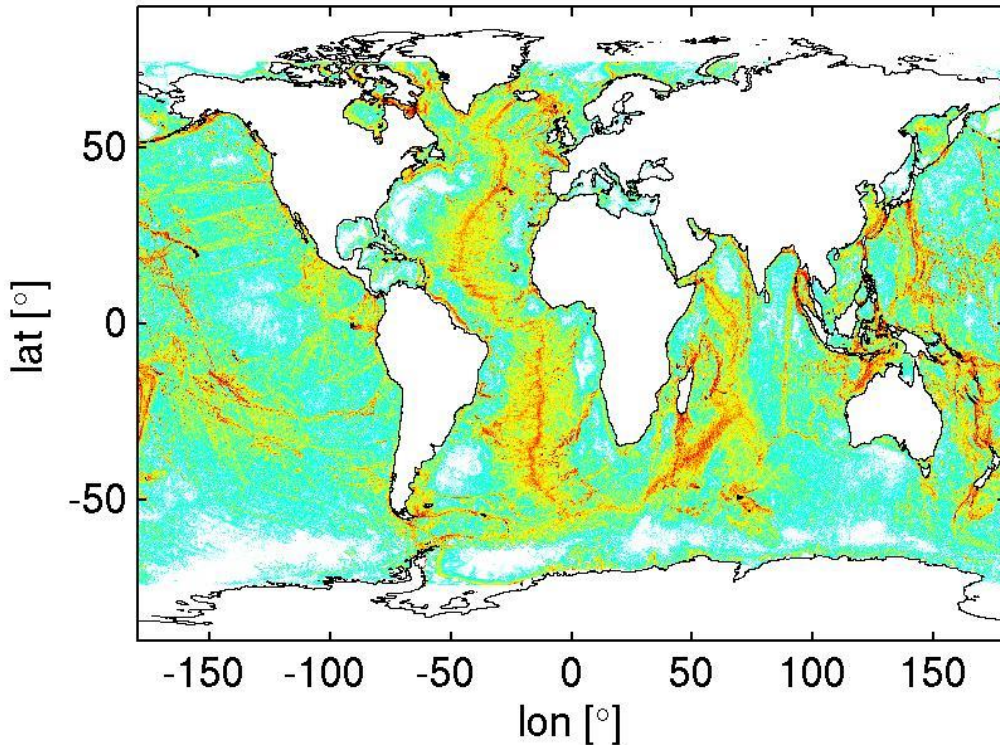
- N from GDEM and h from 30" GEBCO.

Internal Wave Drag Schemes

| study | type | Characteristics | Scale factor range | Name |
|------------------------------------|--------|---------------------------------|--------------------|------------------------|
| Jayne and St Laurent (2001) | scalar | full | 0.25 – 0.75 | JSL |
| Nycander (2005) | tensor | full | 0.5 – 4 | full tens |
| Nycander (2005) | scalar | full | 0.5 – 4 | full scalar |
| Nycander (2005) | tensor | reduced at supercritical slopes | 0.5 – 8 | tens no supercr |
| Nycander (2005) | scalar | reduced at supercritical slopes | 0.5 – 6 | scal no supercr |
| Nycander (2005) | scalar | reduced above 2000 m | 1 – 5 | lim scal 2km |

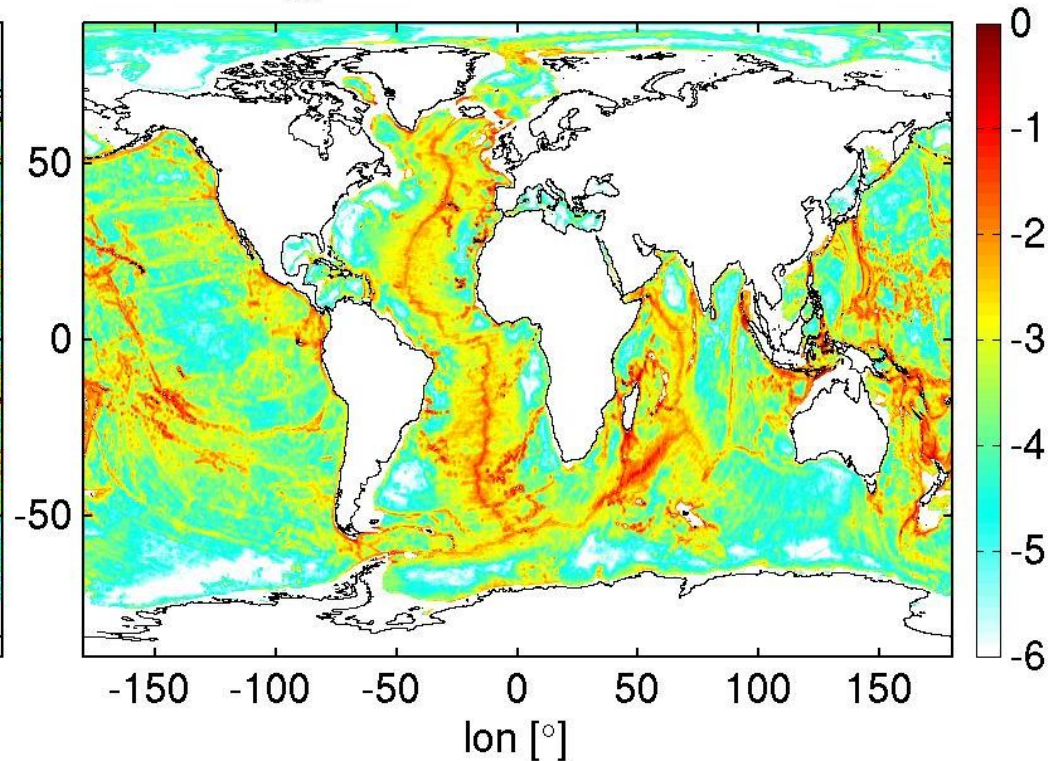
Internal Wave Drag Schemes

$\log_{10}(D_{lin})$ [Wm^{-2}]; full tens; scalefac. = 1.5



Nycander tensor

$\log_{10}(D_{lin})$ [Wm^{-2}]; JSL; scalefac. = 0.375



JSL scalar

Validation

- Compare HYCOM and TPXO8 M_2 water levels

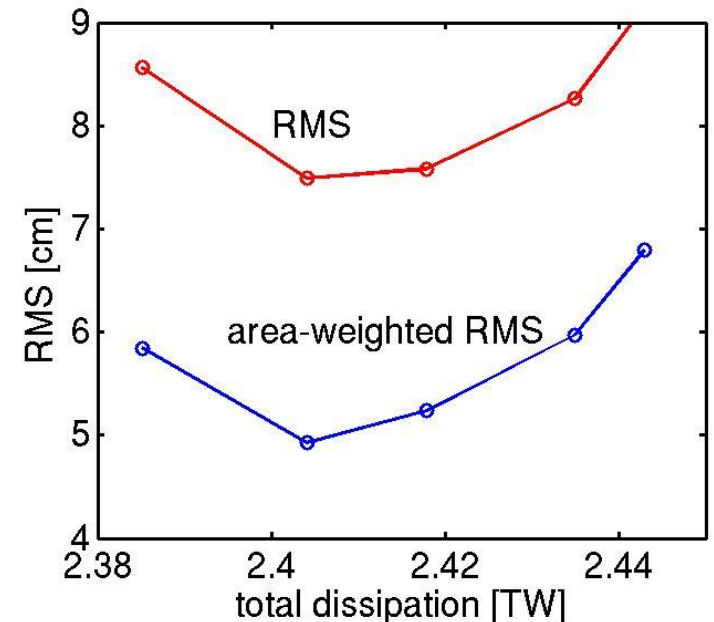
- error in each grid point

$$RMS_t = \sqrt{\frac{1}{T} \int (\eta_m - \eta_o)^2 dt} = \sqrt{\langle (\eta_m - \eta_o)^2 \rangle}$$

- global mean

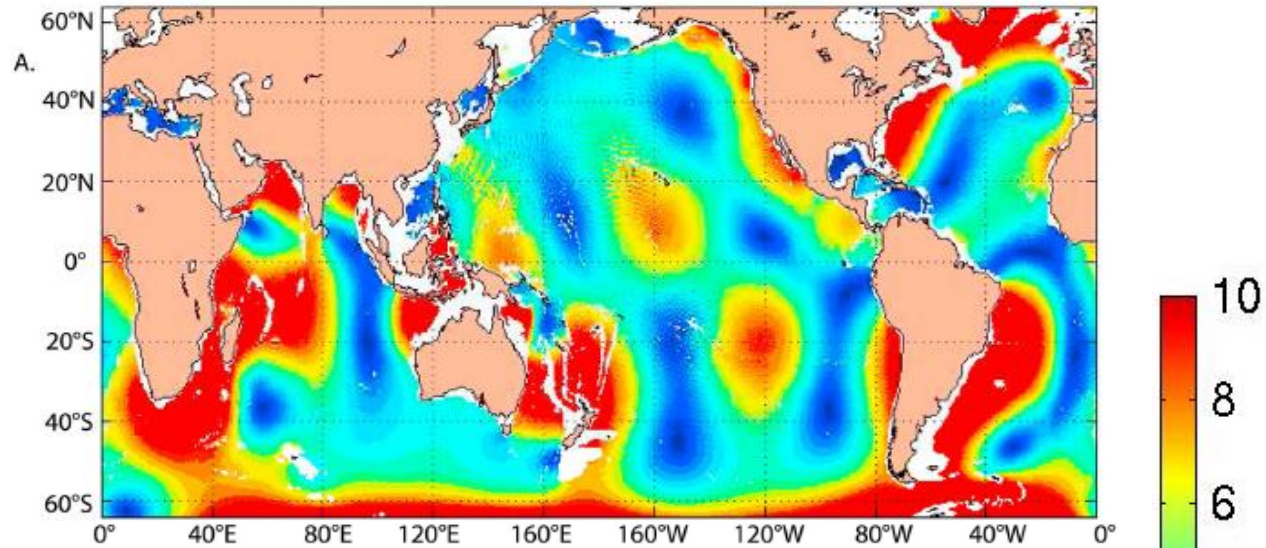
Method 1) $RMS = \sqrt{\frac{\int RMS_t^2 dA}{\int dA}}$

Method 2) $RMS_A = \frac{\int RMS_t dA}{\int dA}$

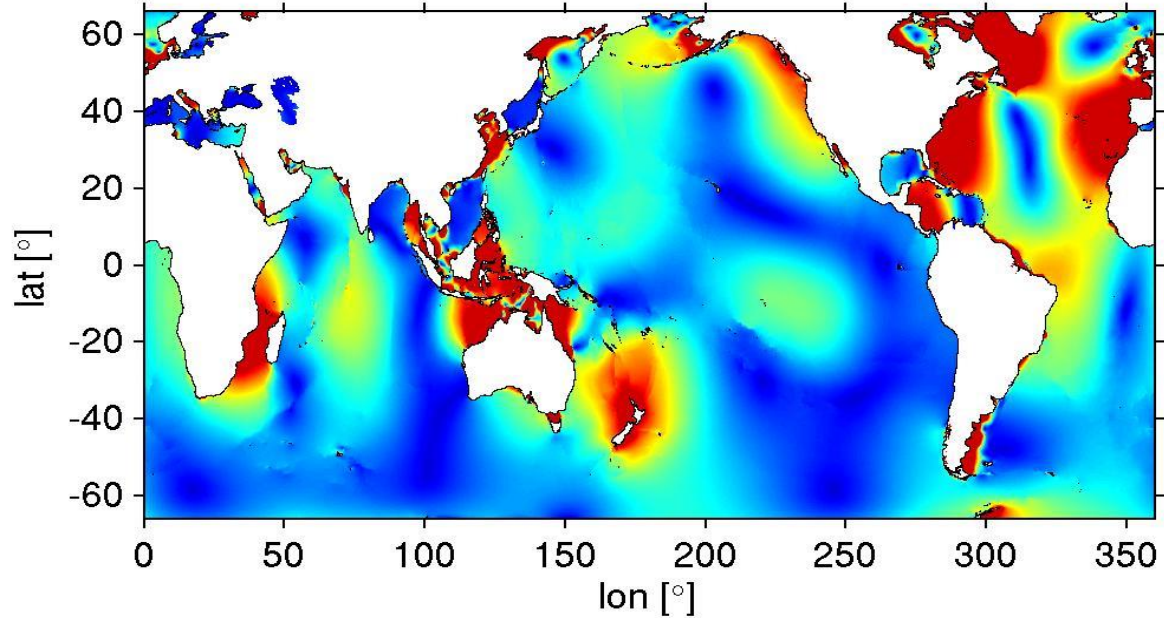


RMS_t

Previous 3D HYCOM (Shriver et al, 2012); RMS_A = 7.5 cm



RMS_t [cm] JSL-SAL - TPXO8; RMS_A = 3.66 cm



Validation

- Compare HYCOM and TPXO M₂ mean energy dissipation rates

- TPXO:
$$\boxed{W} - \boxed{\nabla \cdot \mathbf{P}} = D$$

input flux div.

Dissipation rates of TPXO4a, TPXO6.2*, TPXO7.2*, and TPXO8-ATLAS*

*provided by Mattias Green

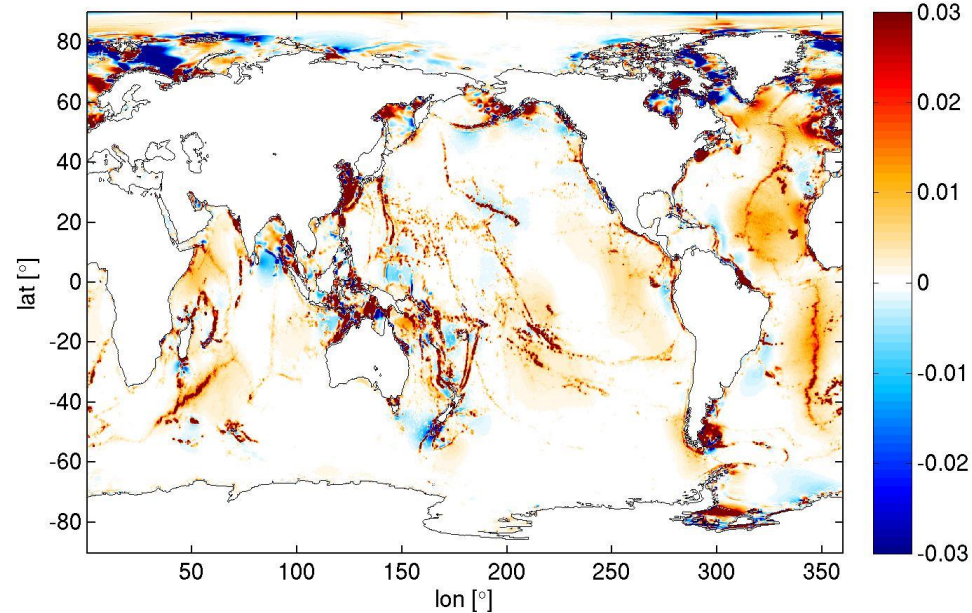
- HYCOM:
$$D = \boxed{\rho_0 \langle \mathbf{u} \cdot \mathbb{C} \cdot \mathbf{u} \rangle} + \boxed{\rho_0 \langle C_D |\mathbf{u}|^3 \rangle}$$

internal w. drag bottom drag

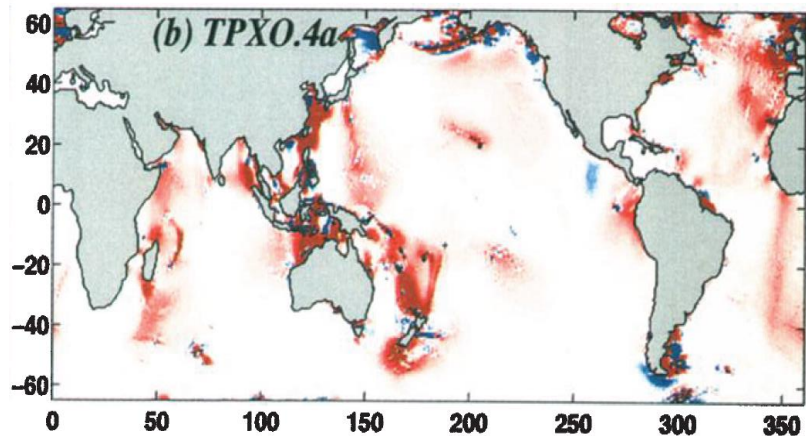
HYCOM rates are the average of the offline and online computations

TPXO Dissipation Maps

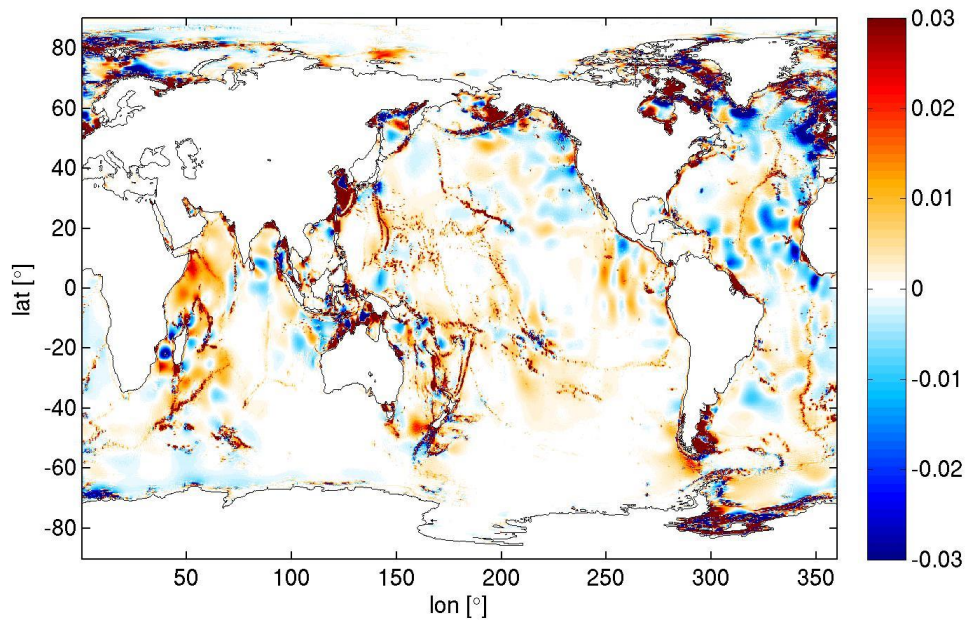
TPX06.2 [W/m²]



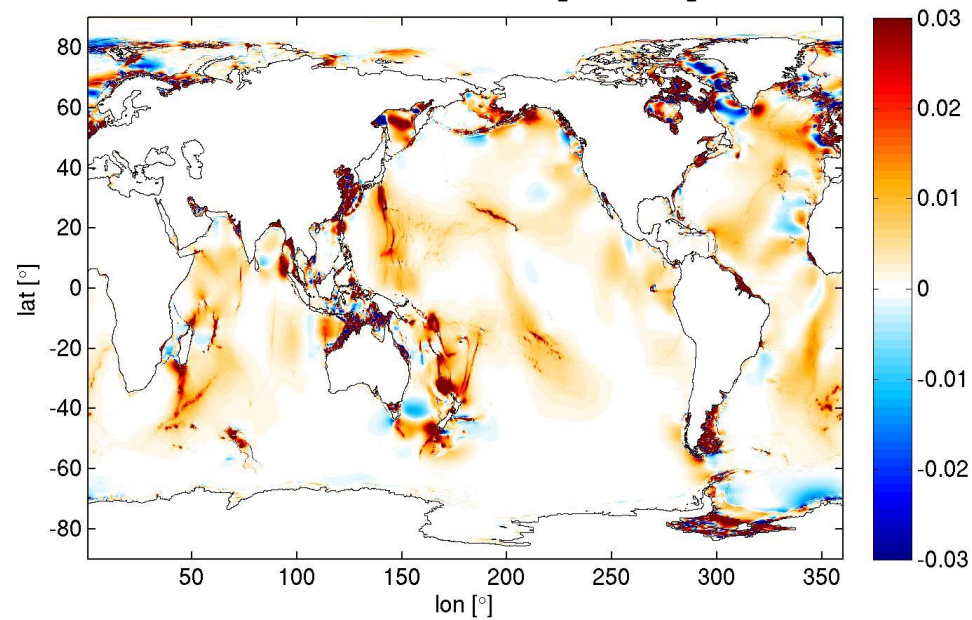
TPX04a



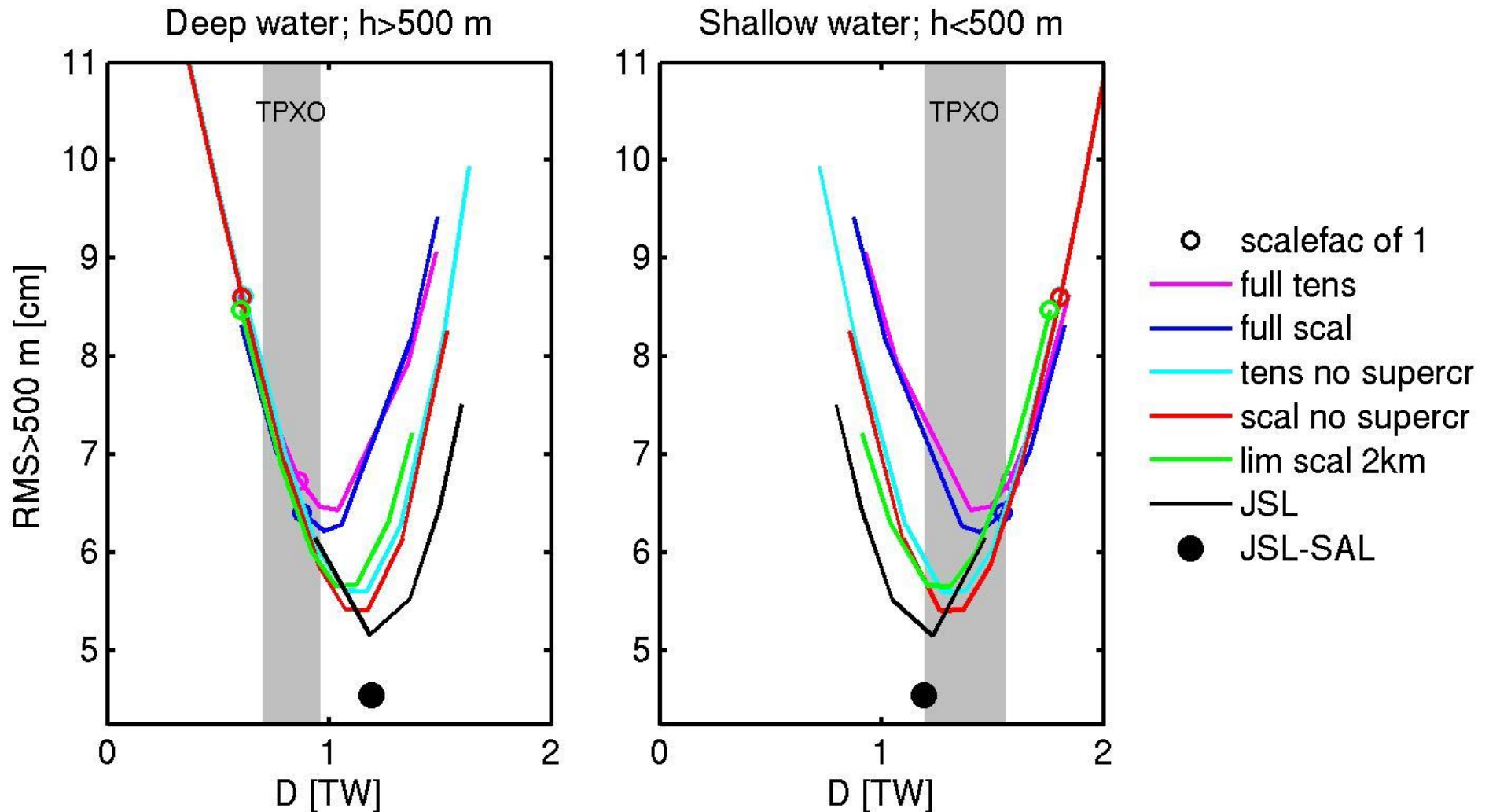
TPX07.2 [W/m²]



TPX08-ATLAS [W/m²]



Global Validation

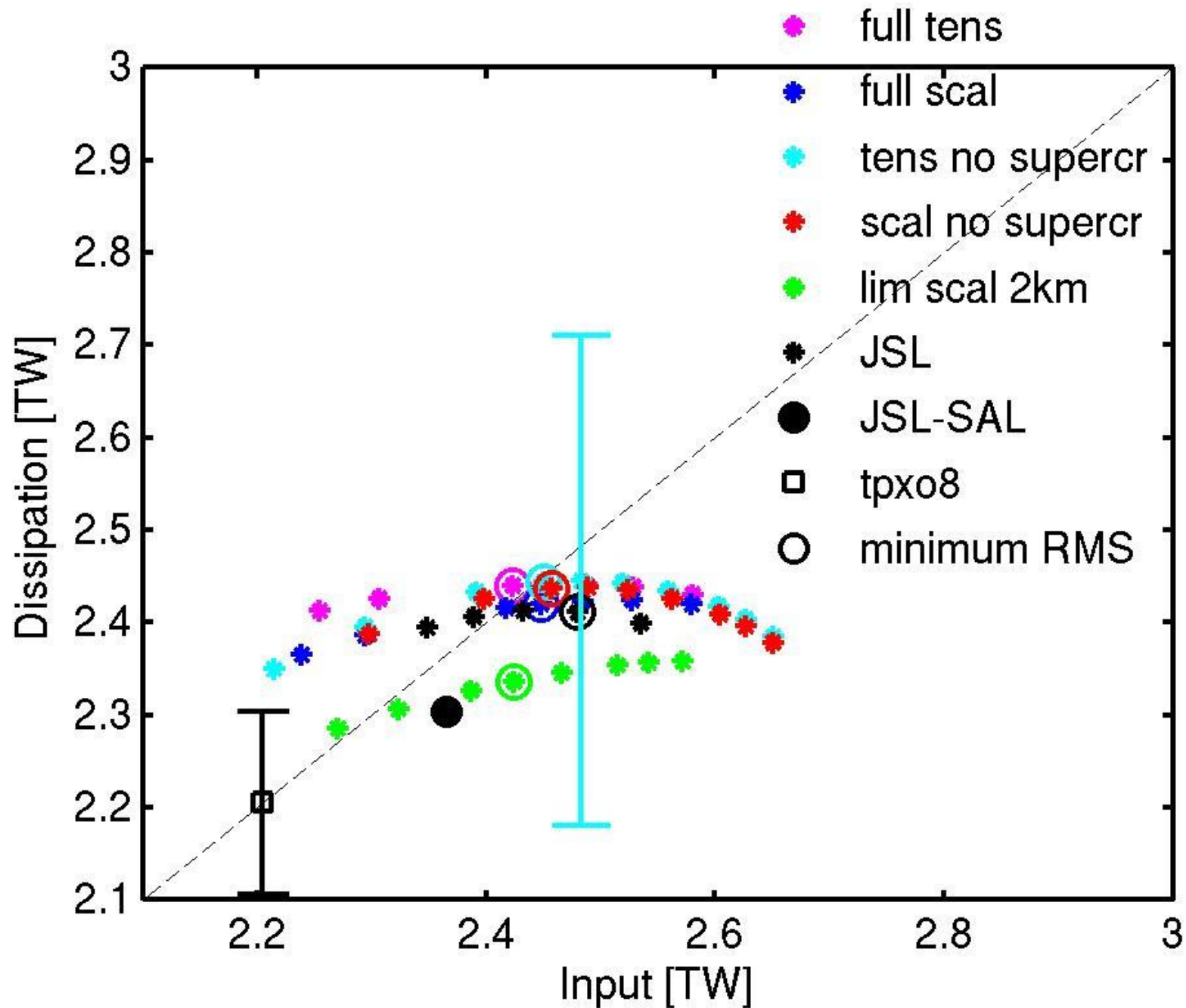


increase in scale factor

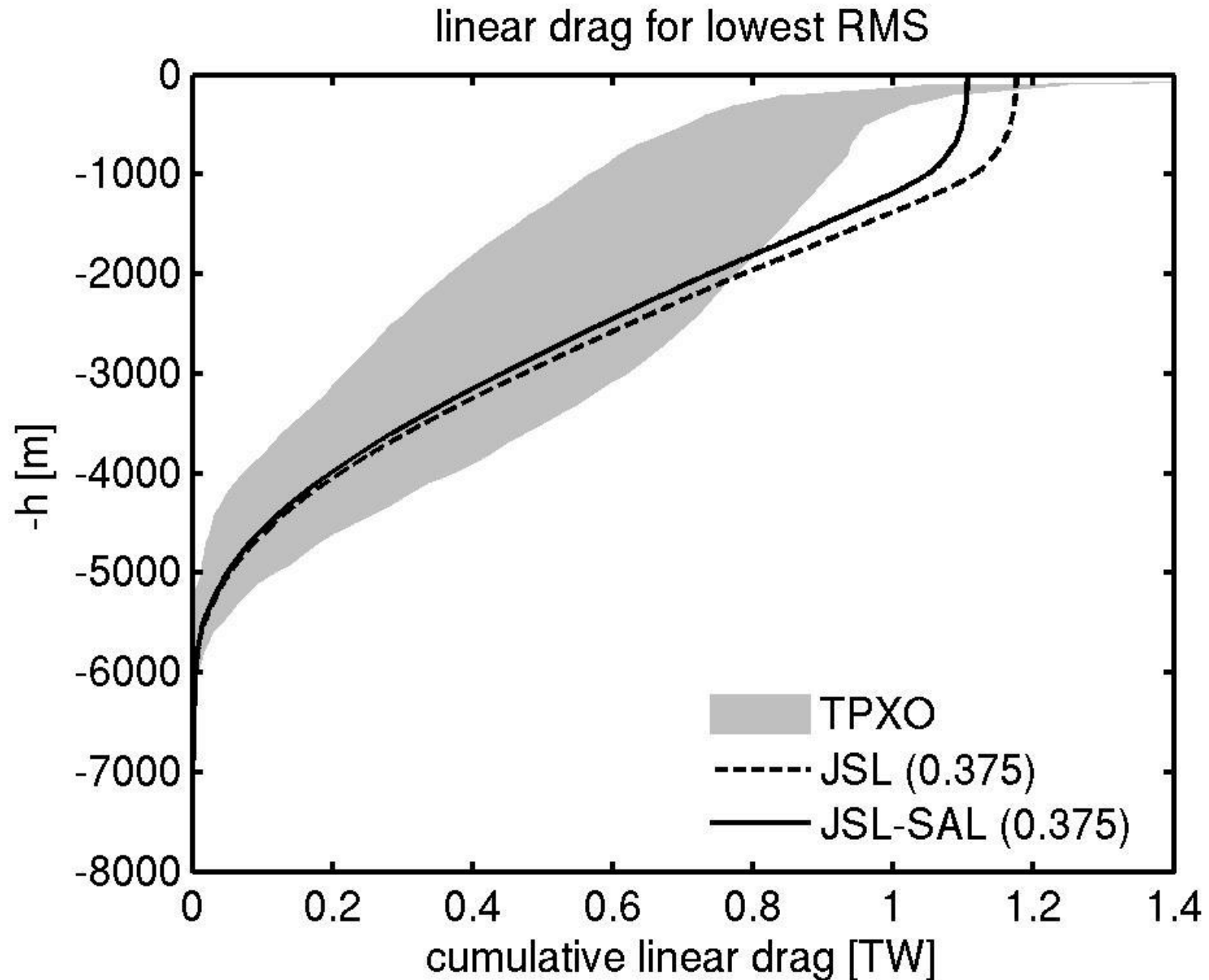


increase in scale factor

Global Validation

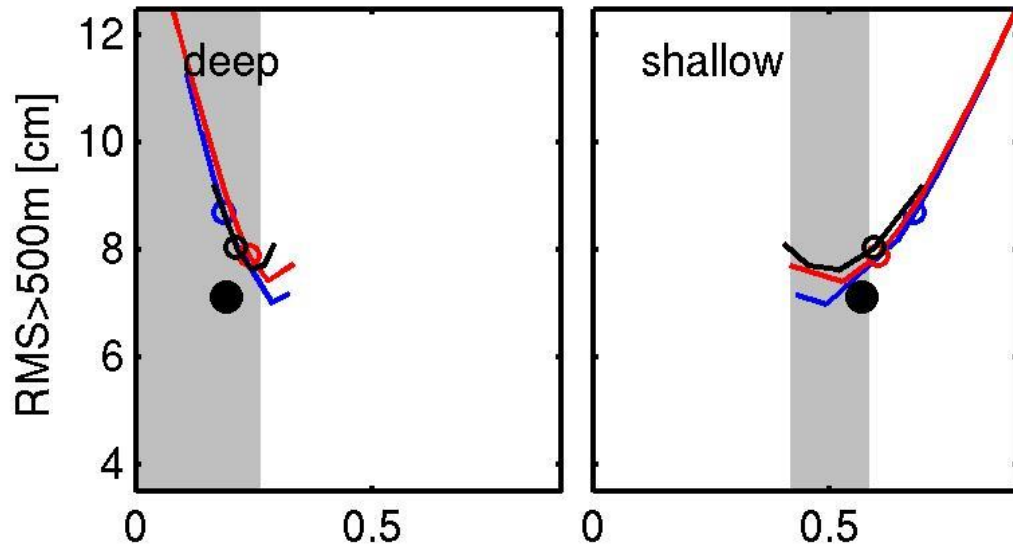


Global Validation

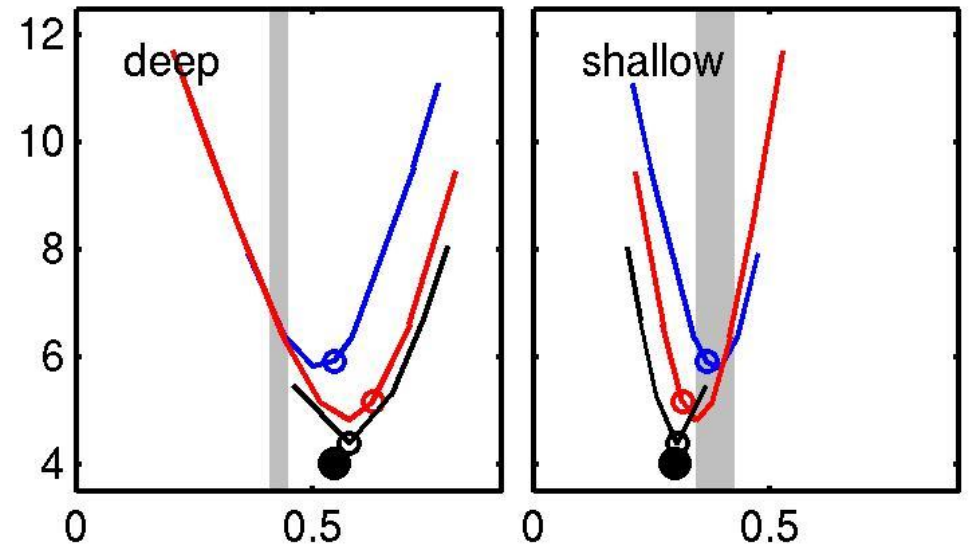


Basin Validation

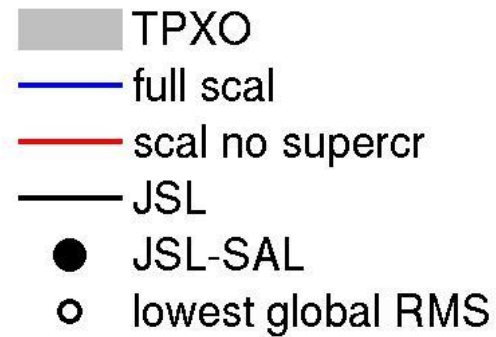
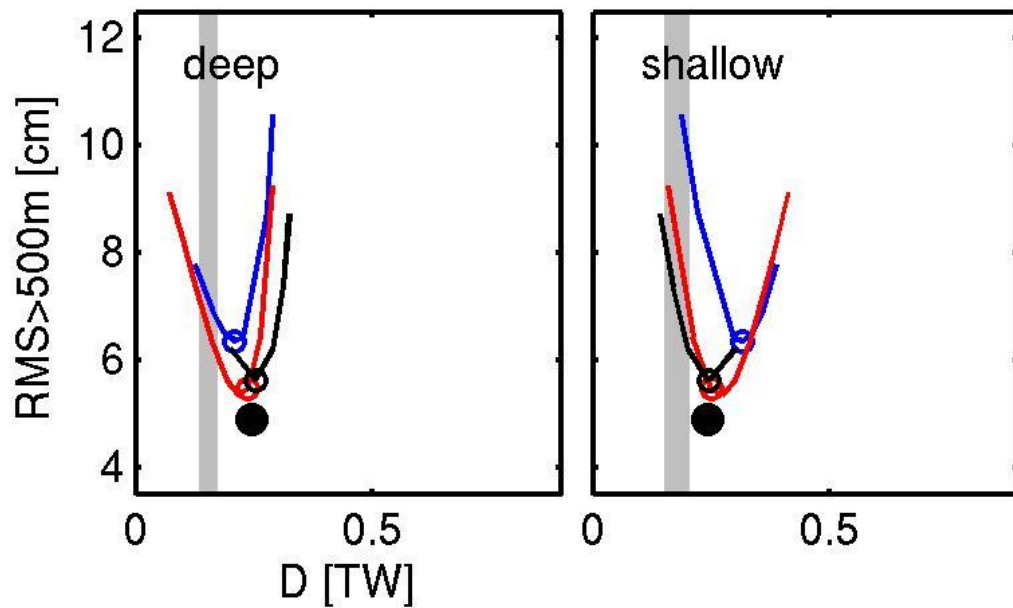
Atlantic



Pacific



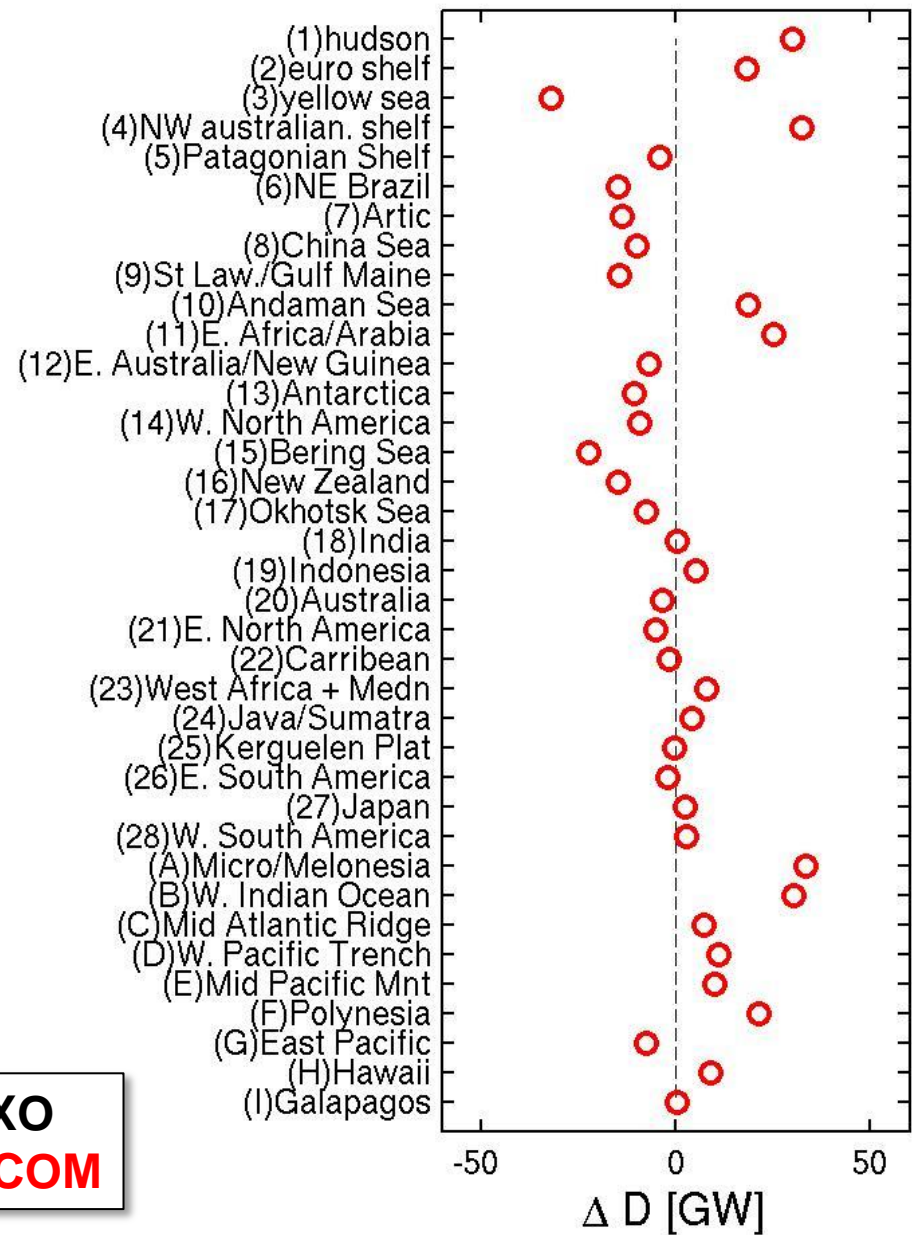
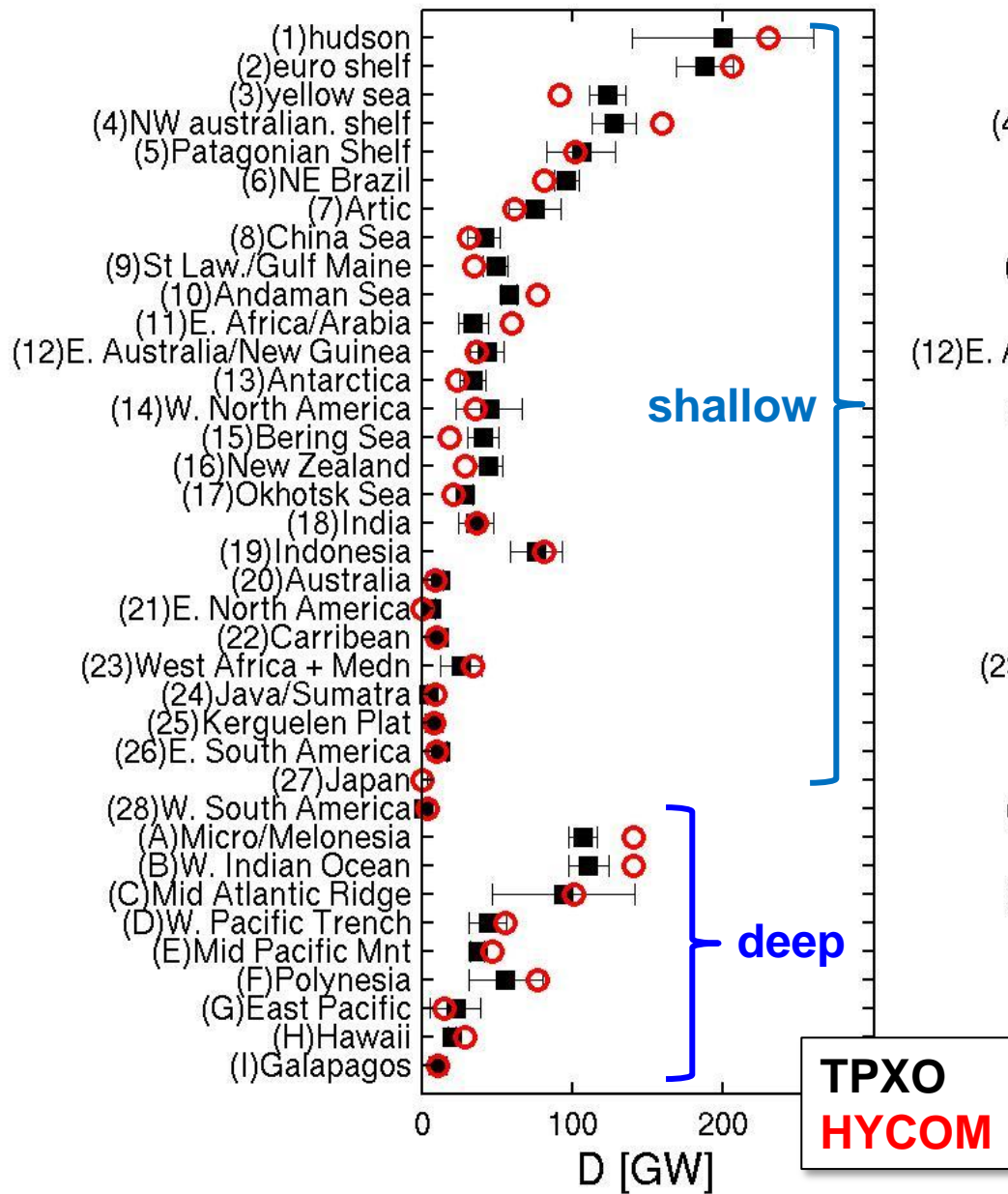
Indian Ocean



Regional Validation

JSL SAL (0.375)

mean= 2 GW; RMS=16 GW



Compare with Past Results

| Model Study | Linear drag | Model (Layers) | Res [°] | Data source | RMS (> 1km) [cm] | Tot. RMS [cm] |
|-----------------------------|-------------|----------------|---------|-------------|------------------|---------------|
| Jayne and St Laurent (2001) | JSL | JSL (1) | 1/2 | UT-CSR | <u>6.7</u> | |
| Arbic et al (2004) | Garner | HIM (2) | 1/4 | GOT99 | 7.3* | |
| Arbic et al (2004) | - | HIM (2) | 1/4 | GOT99 | 17.1* | |
| Simmons et al (2004) | - | HIM (2) | 1/8 | GOT99 | 23.4* | |
| Egbert et al (2004) | Bell | OTIS (1) | 1/12 | TPXO5 | ~5* | ~9* |
| Arbic et al (2010) | Garner | HYCOM (32) | 2/25 | tide gages | 8.3 | |
| Shriver et al (2010) | Garner | HYCOM (32) | 2/25 | TPXO7.2 | <u>7.5*</u> | |
| Muller et al (2012) | - | MPI-OM (40) | 1/10 | tide gages | 8.2 | |
| Green & Nycander (2012) | Nycndr | OTIS (1) | 1/8 | TPXO7.2 | 7.0# | |
| Buijsman et al (2013) | JSL | HYCOM (1) | 2/25 | TPXO8 | 4.5* | 6.8 |
| Buijsman et al (2013) | JSL | HYCOM (1) | 2/25 | TPXO8 | <u>3.6*</u> | <u>4.3</u> |

* equatorward of 66°

area-weighted RMS value

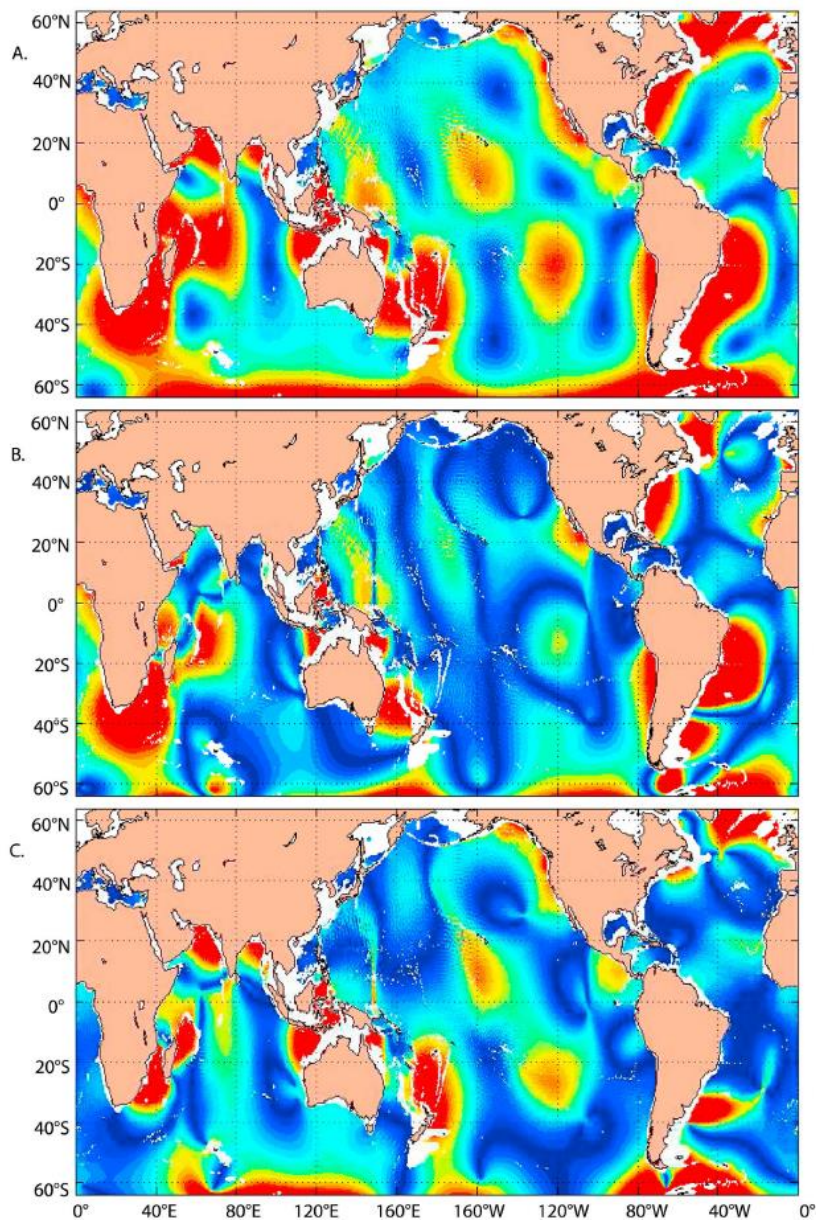
>500 m

Conclusions

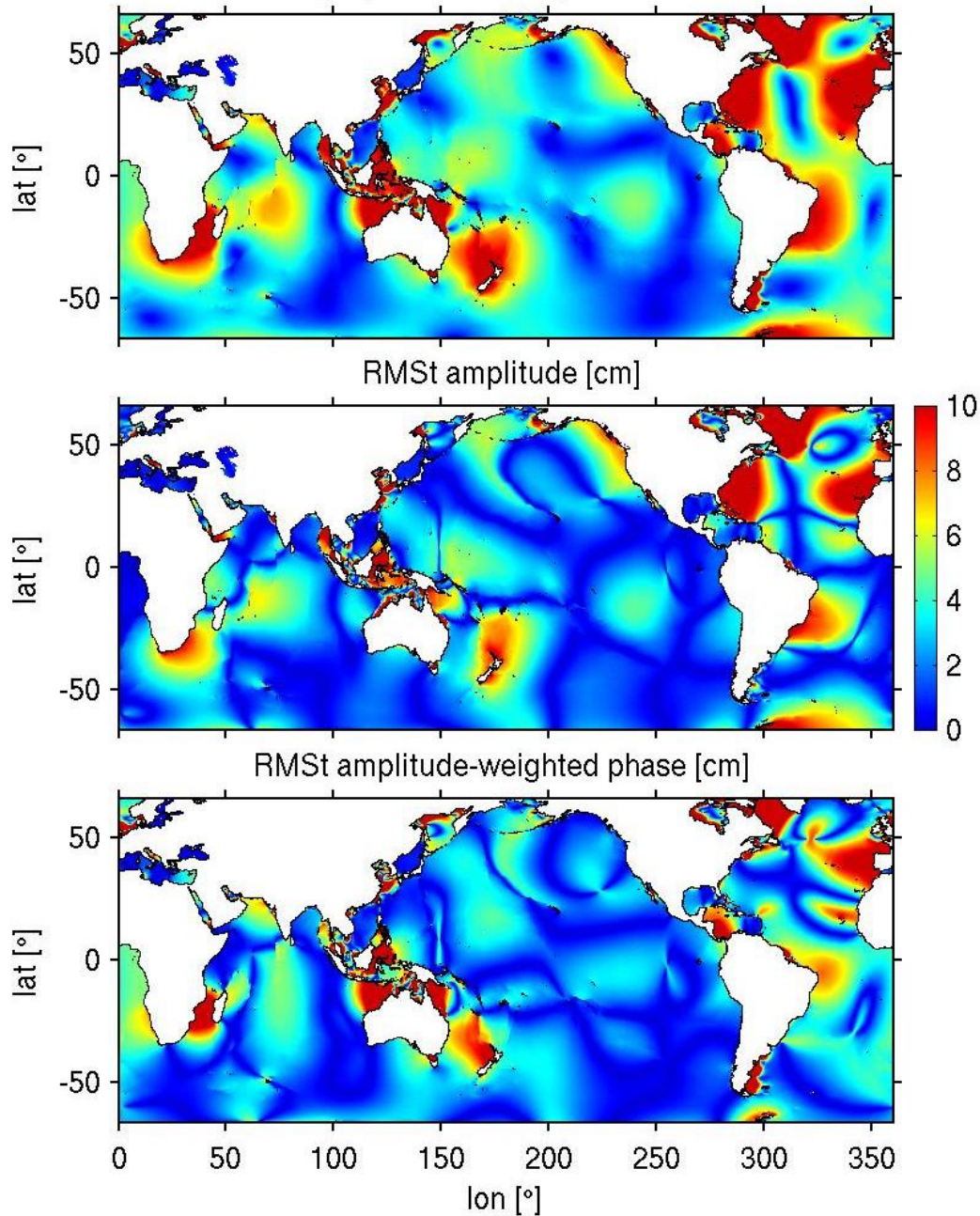
1. To get the best RMS the linear drag needs to be tuned
2. The full Nycander tensor has dissipation rates close to TPXO, but not the best RMS values
3. The Nycander scalar is slightly better than the tensor
4. Increasing the linear drag in deep relative to shallow water improves the water levels, but increases the discrepancy with the TPXO dissipation rates
5. The Atlantic is an outlier: the optimum RMS in the Atlantic is not the optimum RMS in the other basins
6. Iterating the SAL brings the model closer to TPXO

Lowest RMS_t for JSL

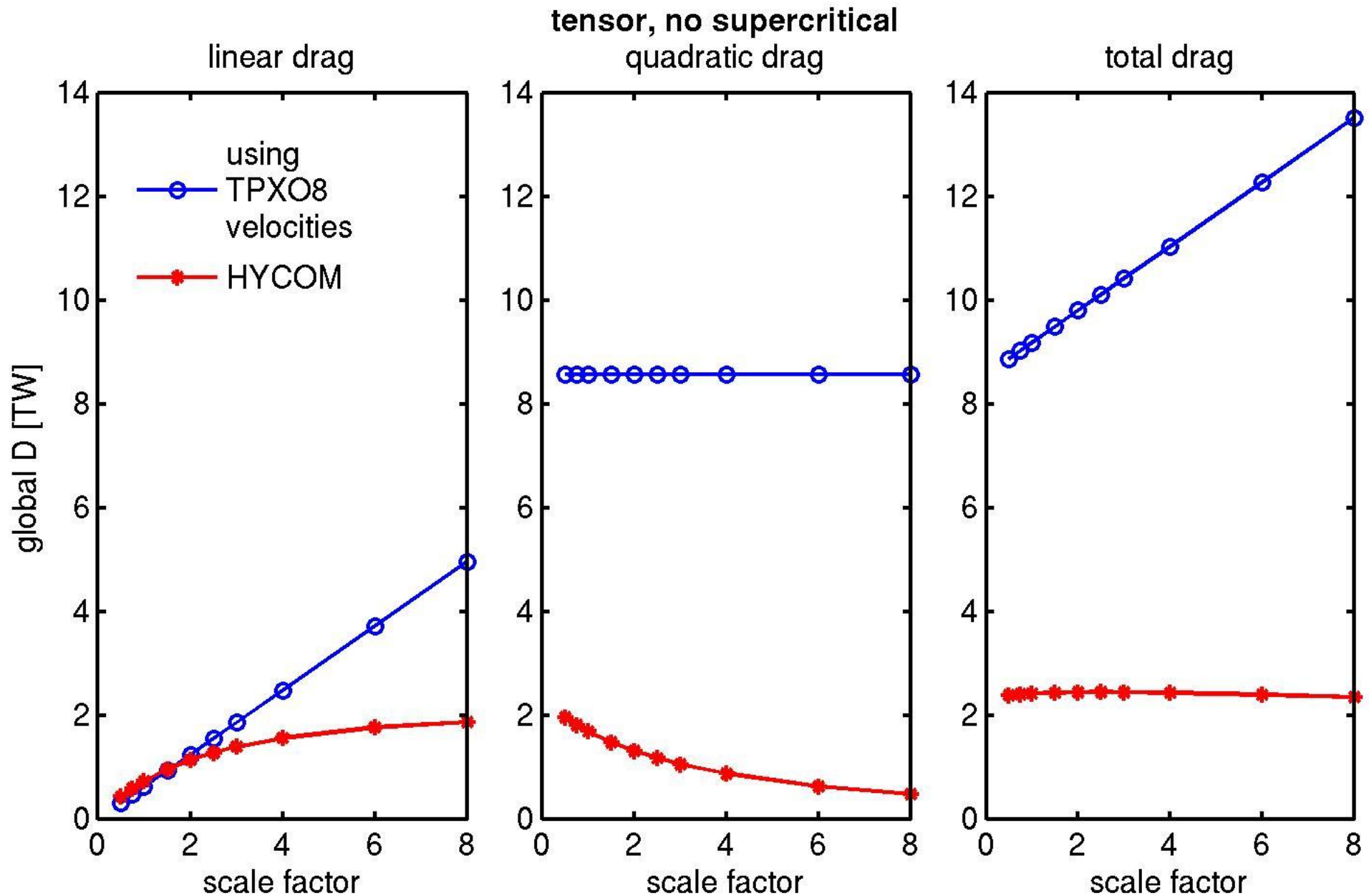
Previous 3D HYCOM; $RMS_A = 7.5$ cm



RMS_t [cm] JSL - TPX08; $RMS = 5.16$ cm



Response to Scale Factor



Internal Wave Drag Schemes

